# Modular forms and their combinatorial variants

Topics in Mathematical Science IV, Nagoya University, Spring 2023

Homepage for this course: https://www.henrikbachmann.com/mf\_2023.html.

• Contact

Name: Henrik Bachmann, Room: 457 (Math. Building). Email: henrik.bachmann@math.nagoya-u.ac.jp (feel free to ask any questions).

#### • Lecture notes:

I will provide lectures notes for the lectures which will be updated during the next weeks. You will find a preliminary version on the homepage in the coming days. Please check the homepage regularly for updates. If you find any typos in the notes please let me know.

### • Lectures

We we will have 15 lectures: 04/14, 04/21, 04/28, 05/12, 05/19, 05/26, 06/02, 06/09 (On this day is medai-sai. Not decided yet if we do lecture this day), 06/16, 06/23, 06/30, 07/07, 07/14, 07/21, 07/28.

(we will not use the make-up days on 05/13 and 06/06)

### • Grading & Exercises:

The grading will be based on written homework assignments. The first homework sheet will appear in TACT in the second week. Be sure to be member of https://tact.ac.thers.ac.jp/portal/site/n\_2023\_3211090 and be aware of TACT announcements.

• Literature:

There are various books on modular forms and lecture notes, which can be found in the library and online. Below you can find a list of standard books, which we will use during the lectures. We will need some tools from complex analysis, which can be found in [FB] or [SS].

## References

- [CS] H. Cohen, F. Strömberg: Modular Forms: A Classical Approach, Graduate Studies in Mathematics, Volume: 179, American Mathematical Society, 2017.
- [DS] F. Diamond, J. Shurman: A first course in modular forms, Graduate Texts in Mathematics, No. 228. Springer-Verlag, New York, 2005.
- [FB] E. Freitag, R. Busam: Complex analysis, Second edition, Universitext, Springer-Verlag, Berlin, 2009.
- [Ki] L. J. P. Kilford: Modular forms. A classical and computational introduction, Imperial College Press, London, 2008.
- [Ko] N. Koblitz: Introduction to elliptic curves and modular forms, Graduate Texts in Mathematics, No. 97. Springer-Verlag, New York, 1993.
- [L] S. Lang: Introduction to modular forms, Grundlehren der mathematischen Wissenschaften, No. 222. Springer-Verlag, Berlin-New York, 1976.
- [S] J.-P. Serre: A course in arithmetic, Graduate Texts in Mathematics, No. 7. Springer-Verlag, New York-Heidelberg, 1973. (Chapter VII)
- [SS] E. Stein, R. Shakarchi: Complex analysis, Princeton Lectures in Analysis, 2. Princeton University Press, Princeton, NJ, 2003
- [Z] D. Zagier: Elliptic modular forms and their applications, first part in "The 1-2-3 of modular forms", Universitext. Springer-Verlag, Berlin, 2008. (available at http://people.mpim-bonn. mpg.de/zagier/files/doi/10.1007/978-3-540-74119-0\_1/fulltext.pdf)